# **1** Induction and AC Circuits

#### 1.1 Formulas

Faraday's law of induction:  $\Delta V = -N\Delta\varphi_B/\Delta t$  where the magnetic flux  $\varphi_B = BA \cos \theta$ Induced emf in a wire moving  $\bot$  to a magnetic field (Hall Effect):  $\Delta V = \epsilon = Blv$ Induced emf in a wire moving in a magnetic field:  $\Delta V = Blv \sin \theta$ Maximum emf in a generator:  $\Delta V = NBA\omega$ Definition of self inductance L:  $\Delta V = -L\Delta I/\Delta t$ Energy stored in an inductor:  $U = LI^2/2$ RL circuit with  $I_0 = 0$ :  $I(t) = I_{max}(1 - e^{-Rt/L})$ AC current RMS value:  $I_{rms} = I_{max}/\sqrt{2}$ Reactance of a capacitor:  $X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC}$ Reactance of a inductor:  $X_L = \omega L = 2\pi fL$ Impedance of a series RLC circuit:  $Z = \sqrt{R^2 + (X_L - X_C)^2}$ Amplitudes:  $V_R = IR, VL = IX_L, V_C = IX_C$ , and  $\epsilon = IZ$ Angular frequency at resonance:  $\omega_0 = 2\pi f = \frac{1}{\sqrt{LC}}$ 

## 1.2 Dropped Steel Beam Problem

A 11.5 m long steel beam is accidentally dropped by a construction crane from a height of 5.41 m. The horizontal component of the Earth's magnetic field over the region is 12.9  $\mu$ T. The acceleration of gravity is 9.8 m/s<sup>2</sup>.

What is the induced emf in the beam just before impact with the Earth, assuming its long dimension remains in a horizontal plane, oriented perpendicularly to the horizontal component of the Earth's magnetic field? Answer in units of mV.

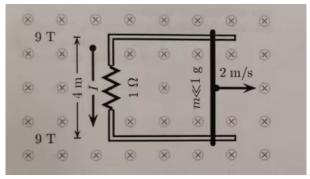
## 1.3 Energy Stored in Inductor Problem

An inductor of 140 turns has a radius of 5 cm and a length of 28 cm. The permeability of free space is  $1.25664\times 10^{-6}~\text{N/A}^2.$ 

Find the energy stored in it when the current is 0.4 A. Answer in units of J.

## 1.4 Force on a Bar Problem

In the arrangement shown in the figure, the resistor is  $1\Omega$  and a 9 T magnetic field is directed into the paper. The separation between the rails is 4 m. An applied force moves the bar to the right at a constant speed of 2 m/s.



Calculate the applied force required to move the bar to the right at a constant speed of 2 m/s. Assume the bar and rails have negligible resistance and friction. Neglect the mass of the bar. Answer in units of N.

## 1.5 Rate of Change of Current in Inductor Problem

An inductor in the form of an air-core solenoid contains 183 turns, is of length 22.7 cm, and has a cross-sectional area of 1.2 cm<sup>2</sup>. The permeability of free space is  $1.25664 \times 10^{-6}$  N/A<sup>2</sup>.

What is the magnitude of the uniform rate of change in current through the inductor that induces an emf of 275  $\mu$ V? Answer in units of A/s.

#### 1.6 Change in Field of Rectangular Coil Problem

The plane of a rectangular coil, 6.9 cm by 3.6 cm, is perpendicular to the direction of a uniform magnetic field B.

If the coil has 75 turns and a total resistance of  $8.9\Omega$ , at what rate must the magnitude of B change to induce a current of 0.04 A in the windings of the coil? Answer in units of T/s.

#### 1.7 Inductor with Series in Lamp Problem

A 0.834 H inductor is connected in series with a fluorescent lamp to limit the current drawn by the lamp.

If the combination is connected to a 67 Hz, 125 V line, and if the voltage across the lamp is to be 46.2 V, what is the current in the circuit? (The lamp is a pure resistive load.) Answer in units of A.